

1.3 Rates of Change and Behaviors of Graphs

A Rate of change describes how the output quantity changes in relation to the input quantity. The units on a rate of change are "output units per input units"

- dollars per hour
- miles per gallon
- beats per second
- farmer plants 60,000 onions per acre

Example 1

t	2	3	4	5	6	7	8	9
$C(t)$	1.47	1.69	1.94	2.30	2.51	2.64	3.01	2.14

The function $C(t)$ above gives the average cost, in dollars, of a gallon of gasoline t years after 2000.

- To find how gas price changed from 2002-2009 you would subtract gas price in 2002 from 2009

$$2.14 - 1.47 = \$0.67 \quad \text{To find average rate of change}$$

$$\text{delta} \longrightarrow \frac{\Delta C(t)}{\Delta t} \longrightarrow \frac{\$0.67}{7 \text{ yr}} = 0.096$$

gas prices increased by about 9.6 cents per year:

$$\text{Average Rate of Change} = \frac{\text{Change of output}}{\text{Change of Input}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$