

Global Risk, Uncertainty and

Volatility Measurement

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Reference notes for Federal Reserve Board talk in Washington, D.C., at their roundtable on "Global Risk, Uncertainty and Volatility."

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Perspectives on Global Risk, Uncertainty and Volatility

1. Volatility is like standard deviation, which picks up **total volatility** of fluctuations, weighting good deviations as much as bad ones.

2. Uncertainty: I think of that as like estimation risk, not being able to identify and estimate factors and to estimate sensitivities to them well (like durations, betas, correlations).

3. Global risk is the main item I examine. I take it to mean examining fluctuations such as increases in unemployment or drops in GDP, wealth or income that clearly hurt a lot of people. It is more "downside risk" or "drawdown risk," as wealth and income and employment fall from prior peak levels.

I. Volatility: Gives equal weight to positive and negative deviations. As low as VIX is, historic volatility is even lower. Traders risk averse.



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II. Uncertainty: Estimation Risk for Major Risk Parameters. Example: Brokers Differ Hugely on Basic Duration Risk for IOs Breeden (1994, Journal of Fixed Income, "Complexities of Hedging Mortgages"

		December	31, 1991(Pa	n Yield	l = 7.55)		December	31, 1994(P	ar Yield =	8.88)
								· ·		
	#1	#2	#3	#5	#6	#1	#3	#4	#5	#6
	Goldman	Prudential	JPMorgan	BS	DLJ	Goldman	JPMorgan	Salomon	BS	DLJ
6.5						1.3			(1.5)	1.9
7.0						(0.4)	(1.9)		(2.7)	0.8
7.5						(1.7)	(3.8)		(4.3)	(0.8)
8.0	(6.4)	(3.7)	(6.1)			(2.6)	(6.1)		(6.0)	(3.1)
8.5	(9.5)	(8.6)	8.9			(2.9)	(7.7)			(2.7)
9.0	(16.8)	(16.8)	12.1			(4.2)	(8.9)		(6.7)	(6.3)
9.5	(22.0)	(16.9)	12.8			(4.9)	(10.0)		(5.6)	(9.9)
10.0	(24.0)	(12.1)	12.1			(4.5)	(11.8)		(5.8)	(15.4)
10.5		(5.7)	(9.6)				(12.9)		(8.2)	
					والمراجع وال					

Broker Forecasts Interest Only Strip Option Adjusted Durations

December 31, 1992(Par Yield = 7.55)

December 31, 1995(Par Yield = 6.79)

	#1	#2	#3	#5	#6	#1	#3	#4	#5	#6
	Goldman	Prudential	JPMorgan	BS	DLJ	Goldman	JPMorgan	Salomon	BS	DLJ
6.5						(6.1)		(17.2)	(16.1)	(5.0)
7.0						(14.9)		(28.1)	(22.0)	(12.2)
7.5						(25.0)		(40.5)	(28.9)	(21.5)
8.0	(4.0)	(8.1)	(9.0)			(33.9)		(37.7)	(34.5)	(40.8)
8.5	(7.4)	(12.4)	(15.0)	(7.3)		(23.4)		(22.3)	(25.1)	(61.2)
9.0	(17.3)	(14.7)	(18.0)	(7.6)		(19.4)		(17.9)	(13.7)	(12.6)
9.5	(22.8)	(12.5)	(17.0)	(8.8)		(14.5)		(15.4)	(9.0)	(10.9)
10.0	(28.3)	(8.6)	(12.0)	(9.0)		(10.7)		(13.2)	(7.4)	(11.8)
10.5		(5.9)	(8.0)	(12.4)				(12.6)	(8.5)	

December 31, 1993(Par Yield = 6.67)

June 30, 1996(Par Yield = 7.80)

1										
	#1	#2	#3	#5	#6	#1	#3	#4	#5	#6
	Goldman	Prudential	JPMorgan	BS	DLJ	Goldman	JPMorgan	Salomon	BS	DLJ
65					(13.3)	1.3			(1.5)	1.9
70	(22.4)	(17.0)	8.5		(16.5)	(0.4)		(1.9)	(2.7)	0.8
75	(34.6)	(27.8)	9.8		(26.8)	(1.7)		(3.8)	(4.3)	(0.8)
8.0	(41.6)	(32.4)	11.5		(31.3)	(2.6)		(6.1)	(6.0)	(3.1)
85	(11.3)	(17.4)	3.8		(26.7)	(2.9)		(7.7)		(2.7)
90	(5.8)	(14.1)	(5.1)	(12.4)	(24.2)	(4.2)		(8.9)	(6.7)	(6.3)
9.5	(5.6)	(11.0)	(5.1)	(12.5)	(24:7)	(4.9)		(10.0)	(5.6)	(9.9)
10.0	(4.1)	(6.1)	(0.6)	(12.1)	(24.5)	(4.5)		(11.8)	(5.8)	(15.4)
10.5			4.7	(14.8)				(12.9)	(8.2)	

Uncertainty: Estimation Risk. Brokers Differ Hugely on Option Costs for Mortgage Interest Only Strips (IOs). Sign even differs!



Exhibit 11a





4 Brokers: 9.0% Interest Only Option Costs Monthly September 1991 - June 1996





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III. Measuring Global Risk: <u>A Simple and Intuitive Model: SBCLI</u>

"A Stocks, Bonds, Consumers Leading Indicator"

Source: Breeden (2011-2016)

Risk is used here to be downside risk, or drawdown from peak risk, where many people are hurt by the fluctuations, after they were accustomed to prior living habits.

Unemployment Drawdowns Identify the Most Serious Recessions



Stock price drops from peak (drawdowns) do not seem to Measure real economic pain as much as macro drawdowns



<u>A Stocks, Bonds, Consumers Leading Indicator (SBCLI©)</u> <u>With Only Three Key, Intuitive Factors In Forecasting,</u> <u>We Can Do Nearly As Well As The 10 Factor LEI</u>

- **S.** <u>Stocks</u>: Stock market prices reflect profit forecasts, which are related to forecasted economic growth.
- B. <u>Bonds</u>: Term structure slope (long term rate short term rate, e.g., 10 year rate 3 month rate) predicts increases and slowdowns in economic growth for advanced economies with little credit risk. For emerging economies, sovereign bond credit spreads over USA are used as leading indicators.
- Consumers: Consumers make thoughtful, intelligent choices.
 Consumption growth that is independent of stock market returns reflects consumers' views of jobs, incomes and investment opportunities.

Source: "A Stocks, Bonds, Consumers Leading Indicator," Breeden 2016

<u>Standardized Z-Scores for Real Stock Returns,</u> <u>Term Structure Slope, & Consumption Deviations</u>

■ For key variable k (k = Stocks return, bond slope, consumer deviation) at time t: $Z_{kt} = (x_{kt} - \mu_k) \sigma_k$

For a normal distribution, Abs(Z)>1 about 1/3 time, Abs(Z) >2 about 5% time

Simple Stocks, Bonds, Consumers (SBCLI) index proposed is (for advanced economies):

SBCLI = 2*Z(RIStock) + 1*Z(Slope) + 1* Z(Cons Dev'n)





In the 3 Mega-Economies (America, Europe, AustralAsia), the SBCLI

shows a significant leading relationship with GDP and Unemployment.



G-7 Economies

Impact of Consumer Signal on Explanatory Power: Correlation of Forecasts with Actuals 2 to 4 Quarters Later Standard Period from 2007Q1-2015 Q1 Covering the Great Recession of 2008/9 and Sovereign Debt Crisis 2011-2015

	Begin	2-Quart	er Foreca	sts			4-Quart	er Forecas	sts		
	Date:	Stocks +	Stocks +	Stocks,	OECD*	SBCLI-	Stocks +	Stocks +	Stocks,	OECD*	SBCLI-
	Ending:	Bond	Consumers	Bonds	Leading	LEI	Bond	Consumers	Bonds	Leading	LEI
G-7 Country	2015-Q2	Slope		Consumers	Indicators		Slope		Consumers	Indicators	
United States	2007-Q1	0.68	0.77	0.77	0.74 *	0.03	0.57	0.66	0.74	0.64 *	0.10
Canada	2007-Q1	0.56	0.54	0.60	0.69 **	-0.09	0.46	0.24	0.42	0.55 **	-0.13
France	2007-Q1	0.60	0.66	0.64	0.65	-0.01	0.63	0.58	0.66	0.63	0.03
Germany	2007-Q1	0.55	0.53	0.52	0.57	-0.05	0.51	0.43	0.52	0.48	0.04
Italy	2007-Q1	0.49	0.56	0.54	0.58	-0.04	0.55	0.51	0.57	0.54	0.03
United Kingdom	2007-Q1	0.64	0.63	0.69	0.56	0.13	0.58	0.42	0.57	0.54	0.03
Japan	2007 <i>-</i> Q1	0.46	0.45	0.44	0.41	0.03	0.33	0.38	0.38	0.21	0.17
Averages		0.57	0.59	0.60	0.60	0.00	0.52	0.46	0.55	0.51	0.04

*For USA, Conference Board's LEI is used, as it has higher correlations than the OECD's Leading Index.

**For Canada, note that the MA2 forecasts for Stocks and Bond's and SBCLI are worse than not using the moving average. Use of just the latest observation would increase correlations from 0.56 to 0.63, 0.54 to 0.73 and 0.60 to 0.72, respectively, and 0.46 to 0.50, 0.24 to 0.48, and 0.42 to 0.56 for 4 quarter forecasts.

SBCLI Predicts Major Drawdown Risk Better Than VIX

	United States	Correlations		9/23/2017 10:46
	Hist Vol L12	Hist Vol L24	VIX Eoqm	SBCLI MA2
Real Stock Mkt Drawdown %	-0.48	-0.46	-0.48	0.37
Next 4Q Chg SP500 Drawdown	0.26	0.31	0.17	0.16
	Hist Vol L12	Hist Vol L24	VIX Eoqm	SBCLI MA2
Unemployment Drawdown	-0.58	-0.64	-0.47	0.42
Next 4Q dUnemploymt Drawdo	-0.11	0.06	-0.31	0.60
	Hist Vol L12	Hist Vol L24	VIX Eoqm	SBCLI MA2
Next 4Q GDP-Trend	0.03	0.02	-0.10	0.53
Next 8Q GDP-Trend	-0.26	-0.15	-0.23	0.79
Next 12Q GDP-Trend	-0.35	-0.35	-0.24	0.63
	Hist Vol L12	Hist Vol L24	VIX Eoqm	SBCLI MA2
Next 12 Mos Volatility	0.28	0.02	0.48	-0.42
Next 24 Mos Volatility	0.14	-0.03	0.32	-0.43

What are 17 Trillion Dollar Global Economies SBCLI Risks Today?

	Summary	of Compor	nents of B	reeder	n's Stoc	ks, Bonc	ls, Cor	sumers	Leading	g Indexe	es for 17	7 TDEs			
			Douglas T	. Breed	len, Duk	e Univers	ity and	Amundi	Pioneer						
	GDP Trend	GDP										9/21/2017	22:59		Implied
	Growth	Sensitivity	Stock Mar	ket Z-S	cores (x	Bond Ma	arket Z-	<u>Scores</u>	Consum	ner Z-Sco	ores	Total SB	<u>CLI</u>		GDP Growth
	10 Yr, Pct	to SBCLI Pt	12/30/16	7/7/17	8/24/17	12/30/16	7/7/17	8/24/17	2016-Q4	2017-Q	2017-Q2	12/30/16	7/7/17	8/24/17	Forecast
United States	1.4	0.50	0.8	2.5	2.6	0.3	-0.1	-0.3	1.8	0.5	0.8	3.0	3.2	3.1	3.0
Canada	1.7	0.41	1.5	1.2	1.3	-0.2	-0.3	-0.3	1.0	1.2	2.3	2.3	3.2	3.3	3.0
Brazil	3.0	1.03	1.6	2.2	4.3	-0.6	-0.1	0.1	-2.1	-2.3	-0.6	-1.1	1.5	3.8	7.0
Mexico	2.3	0.42	-0.5	0.9	1.3	0.0	0.3	0.2	0.7	0.2	0.0	0.2	1.1	1.5	2.9
France	0.7	0.36	1.4	2.4	2.3	-0.3	-0.3	-0.6	0.9	0.9	-0.1	2.1	1.9	1.6	1.3
Germany	1.4	0.66	1.5	2.8	2.5	-0.5	-0.1	-0.6	0.7	0.4	0.6	1.7	3.2	2.5	3.0
Italy	-0.6	0.53	0.8	2.0	2.4	0.0	0.0	0.0	1.3	1.3	1.3	2.1	3.3	3.7	1.4
Spain	0.3	0.91	0.5	2.1	1.9	0.0	0.0	0.0	1.7	1.1	0.6	2.2	2.7	2.6	2.6
United Kingdor	1.0	0.46	2.6	3.3	3.5	0.3	0.2	-0.1	0.9	0.3	-0.3	3.8	3.2	3.1	2.4
Russia	2.4	1.62	1.7	0.0	0.6	-1.2	-1.0	-1.0	-1.0	-0.8	-0.3	-0.5	-1.3	-0.8	1.2
Turkey	3.8	0.76	-0.6	2.0	3.1	0.2	0.3	0.3	0.1	0.0	-0.4	-0.4	1.9	3.0	6.1
Japan	0.5	0.34	1.5	2.1	1.7	-1.1	-1.4	-1.5	0.4	0.1	0.7	0.8	1.3	0.9	0.8
Australia	3.3	0.29	0.9	1.0	1.2	0.7	1.0	1.2	0.2	0.2	-0.2	1.8	1.8	2.1	3.9
South Korea	2.7	0.07	0.0	2.5	2.4	-0.6	0.1	0.1	-0.4	-0.6	-0.4	-0.9	2.1	2.1	2.8
China*	7.0	0.72	0.2	0.3	0.4	0.1	-0.8	-1.2	0.5	0.4	0.6	0.8	0.1	-0.2	6.9
India	7.4	0.34	0.0	1.8	1.9	-0.9	-1.0	-1.1	-1.5	-1.2	-2.0	-2.4	-1.2	-1.2	7.0
Indonesia	5.6	0.40	0.6	1.7	1.9	0.4	0.6	0.6	-0.3	-0.6	-0.6	0.7	1.7	1.9	6.4
*China trend is 3 yea	ars vs. 10 years fo	r other countries.													

III. Summary of SBCLI Measure of Global Risks

- 1. VIX was shown to forecast next 1 year volatility of stock returns better than historic stock volatility, with 0.48 vs. 0.28 correlation. Traders use their information effectively to improve upon historic volatility levels.
- 2. SBCLI is better than VIX at forecasting stock return volatility over the longer, 2-year forward time period with correlation of -0.43 vs. 0.32.
- 3. SBCLI is much better than VIX at forecasting major macroeconomic risks such as changes in the unemployment rate "drawdown" and deviations of real GDP growth from trends. Correlation differences are approximately 0.60 for SBCLI vs. 0.30 for VIX.
- 4. Current SBCLI readings show strong economies in the Americas, Europe and AustralAsia, with many SBCLI readings in the 2.0 to 3.8 range. Only Russia, China and India show slightly below-trend growth forecasts. SBCLI for Brazil, Italy and Turkey have improved most in recent months.

IV. Measuring Global Risks.

How to Find Interest Rate Insurance Prices From Option Prices:

*See Ross (1976), <u>Quarterly Journal of Economics</u> article "Options and Efficiency" and Breeden and Litzenberger (1978) <u>Journal of Business</u> article, "Prices of State-Contingent Claims Implicit in Option Prices." B-L's MIT working paper in 2013 on "Central Bank Policy Impacts on the Distribution of Future Interest Rates" gives the method for calculations in this talk. .

Butterfly Spreads of Caplets and Floorlets

Breeden and Litzenberger (1978, 2014)





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True Probabilities vs.

Insurance Prices or "Risk Neutral Probabilities"

Insurance prices or "risk neutral probabilities" differ from true, objective probabilities, because investors price assets higher for those that pay off most when times are bad (negative beta). Thus, their insurance prices (risk neutral probabilities) exceed their true probabilities.

States that correspond to good economies will have lower insurance prices, and their insurance prices will underestimate the true probabilities.

<u>Equilibrium Price/Probability Ratios</u> <u>In state preference and in CRRA-Lognormal model:</u>

$$\log\left(\frac{\phi_{ts}^{*}}{\pi_{ts}}\right) = \gamma \left[\mu_{t} - g_{ts} - \frac{1}{2}\gamma\sigma_{c}^{2}\right]t$$

 $\frac{\phi_{tr_j}^*}{\pi_{tr_j}} = \frac{E\left[\widetilde{u}_{ts}' \middle| r_j\right]}{E[\widetilde{u}_t']}$

As expected, higher growth states for consumption have lower $\left(\frac{\phi_{ts}^*}{\pi}\right)$ ratios.

(12)

(19)

e

		Illustration	n of True	Probabi	ilities R	elated to	Risk Ne	utral Pro	obabiliti	es_	
True prob	ability = K	*Risk Neutral	x exp(Gam	ma*(gts - r	mu))		Assumes:	CRRA-Log	normal rea	l growth m	odel
Real Grow	/th on Nor	ninal Rate: 19	98 to 2011	Data		Real Grow	th on Nom	inal Rate:	1977 to 19	97 Data	
Intercept	-3.71	(t=-2.2)				Intercept	4.11	(t= 3.2)			
Slope	1.42	(t= 3.8)				Slope	-0.12	(t= -0.8)			
MuCgrow	3					MuCgrowi	3				
		Relative Risk	Aversion (Gamma)				<u>Relative R</u>	isk Aversic	on (Gamma)
Nominal	Real	2	4	8		Nominal	Real	2	4	8	
<u>Rate</u>	<u>Growth</u>	Ratio of True	<u>Probability</u>	<u>v to Risk Ne</u>	eutral*	Rate	<u>Growth</u>	Ratio of Tr	<u>ue Probab</u>	ility to Risk	<u>Neutral*</u>
1	-2.29	0.90	0.81	0.65		1	3.99	1.02	1.04	1.08	
2	-0.87	0.93	0.86	0.73		2	3.87	1.02	1.04	1.07	
3	0.55	0.95	0.91	0.82		3	3.75	1.02	1.03	1.06	
4	1.97	0.98	0.96	0.92		4	3.63	1.01	1.03	1.05	
5	3.39	1.01	1.02	1.03		5	3.51	1.01	1.02	1.04	
6	4.81	1.04	1.08	1.16		6	3.39	1.01	1.02	1.03	
7	6.23	1.07	1.14	1.29		7	3.27	1.01	1.01	1.02	
8	7.65	1.10	1.20	1.45		8	3.15	1.00	1.01	1.01	
9	9.07	1.13	1.27	1.63		9	3.03	1.00	1.00	1.00	
10	10.49	1.16	1.35	1.82		10	2.91	1.00	1.00	0.99	
						11	2.79	1.00	0.99	0.98	
						12	2.67	0.99	0.99	0.97	
						13	2.55	0.99	0.98	0.96	
						14	2.43	0.99	0.98	0.96	
						15	2.31	0.99	0.97	0.95	
*=Up to a	scalar mul	tiple				16	2.19	0.98	0.97	0.94	

"Central Bank Policy Impacts on the Distribution of Future Interest Rates" Breeden and Litzenberger (2014)

2008: U.S. Rate Distribution Transformed from Symmetric to Positive Skewness (Concentrated near zero, but long right tail)



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Summer 2013 Tapering Announcements: Stronger economy shifts distribution towards symmetry



2011 Sovereign Debt Crisis: Draghi ECB cuts rates sharply. Massive shift in Euribor interest rate distribution to positive skewness like U.S.



Draghi Rescues the Euro in 2012 with "Whatever it takes ... "



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V. What are interest rate options markets saying now in the USA, the Eurozone and the UK?

USA Insurance Prices for 3-Month LIBOR in 3 Years

Nov 4 (1.78% 10 Yr), Dec 30 2016 (2.44%), August 29 (2.13%), Sept 15 (2.20%)

Sept 15, 2017: Despite North Korea nuclear, stocks and rates move back up.

3-yr dist'n shifts towards symmetry/normalization.





USA Insurance Prices for 3-Month LIBOR in 8-10 Years Nov 4 (1.78% 10 Yr), Dec 30 2016 (2.44%), Aug 29 (2.13%), Sept 15 2017 (2.20%) Aug 29-Sept 15 2017: NoKo nuclear worries shift long-term dist'n from uniform 0-3.5% to positive skew, high risk premium 0.40 0.35 0.30 0.25 0.20 0.15 0.10 0.05 0.00 <1.5% 4.0% 6.0% 2.0% 3.0% 5.0% 7.0% 8.0% 9%+ Nov 4 2016 Pre-Election Dec 30 2016 Trump Elected X Aug 29 2017 Sept 15 2017



UK Insurance Prices for 3-Month Rate in 3 Years

Jun 23 2016 (1.37% 10 Yr), Aug 12 (0.52%),Dec 31(1.24%), Aug 29 (1.00%), Sept 15 2017 (1.31%) Sept 15 2017: NoKo nuclear worries offset by BoE indications of liftoff in rates. Rate distn shifts higher.





V. Summary: Extracting Interest Rate Insurance Prices from Interest Rate Options Prices

- Using Breeden-Litzenberger butterfly spreads of time spreads of interest rate caps and floors gives interest rate insurance prices. These were shown to reflect major moves by the U.S. Federal Reserve, the European Central Bank and the Bank of England in the Great Recession of 2008-2009 and in the Sovereign Debt Crisis of 2011-2013.
- Insurance prices (Arrow's "state prices") reflect both objective probabilities and marginal utilities in the different economic scenarios.
 Interest rates likely to occur in recessionary economies have higher prices, as they are used to hedge major macroeconomic risks.
- Current pricing in the USA, Eurozone and the UK shows movements towards normalized interest rate distributions in 3, 5 and 8-10 years. However, prices are often very high for very low rate scenarios in 5-10 years, which likely reflects high risk aversion and pricing of recession risks.

VI. Implicit Insurance Prices from Options on Stock Prices for the S&P500.

Breeden and Litzenberger (1978, 2014) technique.

Note: 2005-2006: Low price paid for left tail insurance. High right tail.

		<u>S&P 50</u>	0 Insur	ance Pr	<mark>ices (Ri</mark>	sk-neut	tral den	sity).						
9/22/2017		Monthend	Data from	December	2004. Use	s Breeden-	Litzenberge	er (2014) te	chnique	Option:	12	Months	ттм	
		\$9	90%-\$85 Pu	ts		ATM				\$1	20-\$125 Ca	alls \$1	.10-\$115 Ca	alls
	ATM	S&P 500	Left Tail	90	95	100	105	110	115	120	Right Tail	Sum	Right Tail	Left Tail
Date	Implied σ	Spot Index	Spread	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Spread		Spread	-Right Tail
1/3/2005	14.8	1202.1	14.0%	11.8%	13.7%	13.8%	12.3%	8.4%	7.8%	6.2%	12.0%	100.0%	26.0%	-12.0%
12/30/2005	14.3	1248.3	11.3%	15.4%	17.7%	15.5%	12.0%	7.8%	5.9%	4.2%	10.2%	100.0%	20.3%	-9.0%
6/30/2006	14.5	1270.2	11.5%	16.1%	18.1%	14.5%	11.8%	7.2%	5.8%	4.3%	10.7%	100.0%	20.8%	-9.3%
12/29/2006	14.0	1418.3	10.1%	15.9%	18.6%	15.6%	12.2%	7.7%	5.8%	4.2%	10.0%	100.0%	19.9%	-9.9%
6/29/2007	15.8	1503.4	14.9%	15.8%	16.6%	13.2%	11.0%	6.9%	5.7%	4.3%	11.7%	100.0%	21.7%	-6.8%
12/31/2007	22.2	1468.4	32.7%	13.1%	11.9%	8.5%	7.7%	5.0%	4.4%	3.6%	13.1%	100.0%	21.1%	11.6%
3/31/2008	23.8	1322.7	39.0%	11.9%	10.6%	7.4%	6.9%	4.2%	4.0%	3.3%	12.8%	100.0%	20.1%	18.9%
6/30/2008	22.3	1280.0	34.6%	13.1%	11.6%	8.5%	7.4%	4.8%	4.2%	3.4%	12.3%	100.0%	20.0%	14.6%
9/30/2008	27.0	1166.4	42.7%	10.1%	9.1%	6.4%	6.3%	4.0%	3.8%	3.3%	14.4%	100.0%	21.5%	21.2%
10/31/2008	39.4	968.8	55.0%	6.5%	6.1%	3.8%	4.5%	2.5%	2.8%	2.7%	16.0%	100.0%	21.5%	33.5%
11/28/2008	41.6	896.2	56.3%	6.0%	5.7%	3.7%	4.2%	2.5%	2.8%	2.6%	16.3%	100.0%	21.7%	34.6%
12/31/2008	36.3	903.3	53.9%	7.0%	6.5%	4.3%	4.7%	2.9%	3.0%	2.7%	15.0%	100.0%	20.7%	33.2%
1/30/2009	37.1	825.9	54.2%	7.2%	6.4%	4.3%	4.6%	2.8%	2.9%	2.7%	14.9%	100.0%	20.5%	33.7%
2/27/2009	36.9	735.1	53.6%	7.1%	6.4%	4.5%	4.6%	3.0%	3.0%	2.7%	15.1%	100.0%	20.8%	32.8%
3/31/2009	36.9	797.9	53.1%	6.9%	6.3%	4.6%	4.6%	3.0%	3.0%	2.8%	15.7%	100.0%	21.5%	31.6%
6/30/2009	26.8	919.3	44.8%	10.7%	9.2%	6.6%	6.0%	3.9%	3.5%	3.0%	12.4%	100.0%	18.9%	25.9%
12/31/2009	22.8	1115.1	38.6%	13.0%	11.1%	8.1%	6.8%	4.3%	3.8%	3.1%	11.1%	100.0%	18.1%	20.5%
6/30/2010	28.9	1030.7	48.0%	10.7%	9.0%	5.9%	5.6%	3.2%	3.2%	2.8%	11.7%	100.0%	17.7%	30.3%
12/31/2010	21.4	1257.6	36.9%	14.6%	12.2%	8.4%	7.1%	4.2%	3.7%	3.0%	10.0%	100.0%	16.7%	20.2%
6/30/2011	19.4	1320.6	32.5%	16.8%	13.7%	9.9%	7.4%	4.3%	3.7%	2.9%	8.8%	100.0%	15.4%	17.0%
7/29/2011	20.7	1292.3	35.7%	15.4%	12.7%	8.7%	7.2%	4.1%	3.7%	3.0%	9.7%	100.0%	16.3%	19.5%
8/31/2011	25.3	1218.9	43.4%	12.6%	10.2%	7.2%	6.1%	3.6%	3.4%	2.8%	10.5%	100.0%	16.7%	26.7%
9/30/2011	30.8	1131.4	50.4%	9.4%	8.1%	5.3%	5.3%	3.0%	3.1%	2.8%	12.5%	100.0%	18.4%	32.0%
12/30/2011	24.1	1257.6	42.4%	13.2%	10.8%	7.1%	6.3%	3.6%	3.4%	2.9%	10.4%	100.0%	16.7%	25.8%
6/29/2012	21.0	1362.2	36.8%	16.1%	12.8%	8.6%	6.9%	3.7%	3.4%	2.8%	8.9%	100.0%	15.1%	21.7%
12/31/2012	18.7	1426.2	31.9%	17.1%	14.0%	10.0%	7.6%	4.2%	3.7%	2.9%	8.6%	100.0%	15.2%	16.7%
6/28/2013	17.7	1606.3	30.4%	17.7%	14.8%	10.3%	7.8%	4.6%	3.7%	2.8%	7.9%	100.0%	14.5%	15.9%
12/31/2013	15.2	1848.4	23.3%	19.8%	17.3%	12.8%	8.7%	5.0%	3.8%	2.7%	6.6%	100.0%	13.1%	10.2%

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2017: Risk aversion (Left Tail minus Right Tail) diminished since

China Crash in Aug 2015, but well above risk aversion in 2005-2006

		<u>S&P 50</u>	0 Insur	ance Pr	<mark>ices (R</mark> i	isk-neut	tral den	sity).						
9/22/2017		Monthend	Data from	December	2004. Use	es Breeden-	Litzenberge	er (2014) te	chnique	Option:	12	Months	TTM	
		\$9	90%-\$85 Pu	its		ATM				\$1	.20-\$125 C	alls \$1	.10-\$115 Ca	alls
	ATM	S&P 500	Left Tail	90	95	100	105	110	115	120	Right Tail	Sum	Right Tail	Left Tail
Date	$\text{Implied}\sigma$	Spot Index	Spread	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Butterfly	Spread		Spread	-Right Tail
6/30/2014	14.3	1960.2	20.2%	21.7%	19.2%	13.1%	8.9%	4.7%	3.6%	2.6%	6.0%	100.0%	12.2%	7.9%
12/31/2014	17.3	2058.9	27.0%	21.0%	16.7%	9.8%	7.8%	3.9%	3.5%	2.8%	7.6%	100.0%	13.8%	13.2%
6/30/2015	16.6	2063.1	25.9%	21.8%	17.4%	9.7%	7.9%	3.8%	3.4%	2.7%	7.3%	100.0%	13.5%	12.5%
7/31/2015	15.3	2103.8	22.5%	22.9%	18.9%	10.9%	8.3%	3.8%	3.4%	2.7%	6.7%	100.0%	12.8%	9.7%
8/31/2015	19.8	1972.2	34.0%	18.1%	14.2%	7.9%	7.2%	3.3%	3.4%	2.9%	9.0%	100.0%	15.3%	18.7%
9/30/2015	20.2	1920.0	36.4%	16.0%	13.1%	7.7%	7.2%	4.0%	3.6%	2.9%	9.2%	100.0%	15.7%	20.8%
12/31/2015	17.5	2043.9	27.5%	21.1%	16.7%	8.9%	7.9%	3.6%	3.5%	2.8%	8.0%	100.0%	14.3%	13.2%
6/30/2016	17.0	2098.9	26.1%	22.3%	17.5%	9.1%	7.9%	3.5%	3.4%	2.7%	7.4%	100.0%	13.6%	12.5%
10/31/2016	16.8	2126.2	25.2%	22.6%	17.8%	9.1%	8.0%	3.5%	3.4%	2.8%	7.7%	100.0%	13.9%	11.3%
11/30/2016	16.3	2198.8	23.4%	22.5%	18.2%	10.3%	8.1%	3.7%	3.5%	2.8%	7.4%	100.0%	13.7%	9.7%
12/30/2016	16.4	2238.8	23.5%	22.4%	18.1%	10.6%	8.1%	3.6%	3.5%	2.8%	7.4%	100.0%	13.6%	9.9%
1/31/2017	14.9	2278.9	19.9%	23.4%	19.8%	12.1%	8.5%	3.8%	3.4%	2.7%	6.5%	100.0%	12.6%	7.3%
2/28/2017	14.8	2363.6	19.8%	23.2%	19.8%	12.2%	8.6%	3.8%	3.5%	2.7%	6.5%	100.0%	12.7%	7.1%
3/31/2017	13.9	2362.7	17.5%	23.7%	20.9%	13.0%	8.8%	4.0%	3.5%	2.6%	6.0%	100.0%	12.0%	5.5%
6/30/2017	14.1	2423.4	17.4%	24.3%	21.3%	12.4%	8.7%	3.9%	3.4%	2.6%	6.0%	100.0%	12.0%	5.3%
7/31/2017	12.8	2470.3	13.6%	24.7%	23.2%	14.5%	9.1%	3.9%	3.3%	2.4%	5.2%	100.0%	11.0%	2.6%
8/31/2017	13.9	2471.7	16.4%	24.6%	21.7%	13.0%	8.7%	3.7%	3.3%	2.5%	5.9%	100.0%	11.8%	4.7%
9/15/2017	13.9	2500.2	16.3%	24.8%	21.9%	12.9%	8.7%	3.8%	3.3%	2.5%	5.9%	100.0%	11.7%	4.5%



Freque	ency Di	stributi	on of S	<u>&P 500</u>	Return	is for 3	Sampl	e Perio
	and 5 I	holding	period	ls: (1, 3	, 6, 12,	and 24	month	s)
Low	-9999	-12.5	-7.5	-2.5	2.5	7.5	12.5	
High	-12.51	-7.51	-2.51	2.49	7.49	12.49	9999	
<u>3 Month R</u>	<u>leturn</u>							
1927-2015	57	57	132	235	278	191	107	1057
	5.4%	5.4%	12.5%	22.2%	26.3%	18.1%	10.1%	100.0%
1971-2015	19	26	64	138	154	90	49	540
	3.5%	4.8%	11.9%	25.6%	28.5%	16.7%	9.1%	100.0%
1996-2015	12	17	21	57	81	34	18	240
	5.0%	7.1%	8.8%	23.8%	33.8%	14.2%	7.5%	100.0%
<u>6 Month R</u>	<u>leturn</u>							
1927-2015	90	54	109	123	200	177	304	1057
	8.5%	5.1%	10.3%	11.6%	18.9%	16.7%	28.8%	100.0%
1971-2015	27	29	57	68	124	95	140	540
	5.0%	5.4%	10.6%	12.6%	23.0%	17.6%	25.9%	100.0%
1996-2015	15	15	24	25	60	42	59	240
	6.3%	6.3%	10.0%	10.4%	25.0%	17.5%	24.6%	100.0%
<u>12 Month</u>	<u>Return</u>							
1927-2015	113	62	65	72	94	117	534	1057
	10.7%	5.9%	6.1%	6.8%	8.9%	11.1%	50.5%	100.0%
1971-2015	51	20	30	31	49	70	289	540
	9.4%	3.7%	5.6%	5.7%	9.1%	13.0%	53.5%	100.0%
1996-2015	34	9	6	10	18	35	128	240
	14.2%	3.8%	2.5%	4.2%	7.5%	14.6%	53.3%	100.0%
24 Month	<u>Return</u>							
1927-2015	123	25	31	33	48	60	737	1057
	11.6%	2.4%	2.9%	3.1%	4.5%	5.7%	69.7%	100.0%
1971-2015	55	12	10	15	22	28	398	540
	10.2%	2.2%	1.9%	2.8%	4.1%	5.2%	73.7%	100.0%
1996-2015	43	7	4	5	9	7	165	240
	17.9%	2.9%	1.7%	2.1%	3.8%	2.9%	68.8%	100.0%

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Insurance Prices from S&P 500 Options 2015-2017 vs. Historic Frequencies Show High Risk Aversion in 1-year Options. *Investors pay up to hedge against stock market, economy falls.*



VI. Summary: Risk Aversion Evident in Stock Market Insurance Costs from S&P 500 Options.

- In 2005-2006, Stock market insurance prices implicit in S&P500 options showed little risk aversion, as prices for "right tail" moves (stock prices up 12.5%+) were greater than for insurance against "left tail risks," falls of 12.5%
- From 2008-2017, prices of left tail insurance were higher than for right tail upside bets, presumably reflecting payment for hedges against sharp falls in stock prices and associated poor economies. In extreme times such as the Great Recession, the Sovereign Debt Crisis and the China stock market crash, these price differentials were huge (e.g., 50%-20%=30%).
- Post August 2015 (China stock crash), risk aversion has diminished and prices of left tail risk have dropped. Risk aversion appears higher than 2005/2006, perhaps reflecting memories of the Great Recession and Sov Debt Crisis.
- Insurance prices for falling stock prices are substantially above those for rising stock prices, despite historical frequency distributions opposite.

Appendix: SBCLI for 17 Trillion Dollar Economies 2006-2017

					Stocks, Bonds, Consumers Leading Indicators Douglas T. Breeden, Duke University and Amundi Asset						Cators (SBCLI©) (2Q Returns, Growth)							
Douglas T. Breeden, Duke University and Amundi Asset Management 9/21/2017 2									017 22:59									
	United St Americas	Canada Br	razil	Mexico	France <i>Europ</i> e	Germany	Italy	Spain	United Kingdol FTSE 100	Russia	Turkey	Japan <i>I</i> AustralAsia	Australia N	South Kor C	China	India	Indonesia	United Kingdom FTSE 250
2006-Q4	-1.3	-1.2	1.7	2.4	-1.9	0.5	0.8	1.6	-2.1	2.6	-2.3	-0.3	-0.2	-0.8	2.7	1.7	3.6	
2007-Q1	-0.9	-0.8	4.0	3.4	0.4	-0.6	1.5	2.0	-1.0	3.2	-0.7	1.9	3.3	0.0	3.8	2.1	4.3	
2007-Q2	-2.8	0.1	4.4	3.1	0.4	-1.7	0.6	-0.4	-0.3	2.7	0.0	1.0	2.5	0.9	4.2	1.0	3.7	
2007-Q3	-2.9	0.2	3.1	1.5	-1.1	-0.5	-1.6	-1.4	-1.1	2.5	1.0	-1.5	-0.3	2.4	1.8	2.6	4.6	
2007-Q4	-3.1	0.5	3.6	-0.5	-3.5	-3.3	-3.1	-0.8	-2.2	3.0	0.8	-2.6	-0.1	0.8	-0.4	4.7	5.3	
2008-Q1	-4.4	0.8	3.5	-0.8	-7.0	-5.1	-4.1	-2.1	-4.6	1.7	-2.4	-2.7	-4.1	-3.2	-2.5	2.1	3.5	
2008-02	-3.4	-1.4	2.0	0.3	-7.0	-5.5	-3.8	-4 4	-5.6	1.3	-4 1	-2.8	-7.3	-4 1	-2.9	-2.0	-0.9	
2008-03	-3.7	-24	0.9	-1.3	-5.7	-4.8	-4 1	-5.7	-6.6	0.0	-3.5	-2.9	-7.2	-4 4	-1 9	-4.5	-3.4	
2008-Q4	-7.5	-7.4	-4 1	-6.4	-8.5	-7.3	-6.7	-6.7	-10.6	-4.4	-5.7	-5.6	-8.0	-9.2	0.2	-6.0	-6.4	
2009-Q1	-6.3	-6.6	-3.5	-77	-5.6	-4.2	-6.6	-5.0	-6.8	-5.4	-4.2	-5.6	-5.6	-4.8	11	-6.5	-3.2	
2009-02	0.3	3.1	5.7	-14	14	2.0	-1.3	-2.3	-0.3	16	12	0.8	2.0	5.0	3.8	0.6	4.2	
2009-Q3	4.5	7.0	74	5.3	54	3.3	3.5	22	37	17	5.6	3.6	6.0	77	43	3.9	5.4	
2009-04	4.0	48	37	54	5.9	3.1	3.3	32	62	-0.1	37	11	47	3.8	2.5	12	15	
2010-Q1	1.4	3.5	1.8	2.3	4.4	2.8	1.0	-0.7	3.3	0.9	1.1	0.8	2.2	1.6	2.1	0.8	-0.6	
2010-02	12	2.5	0.1	0.7	07	14	-14	-27	14	-0.4	0.7	0.9	-0.1	0.8	15	-0.6	0.0	
2010-Q3	0.6	1.0	0.5	0.7	-0.4	0.6	-0.6	-2.5	0.6	-0.6	0.8	-0.2	-0.6	1.0	0.3	-17	-0.6	
2010-Q4	27	23	2.5	24	1.9	1.9	0.9	-1.5	0.4	0.8	12	-1 1	0.5	1.8	0.5	-0.1	0.5	
2011-01	4.3	2.3	1.6	19	3.7	3.8	0.9	-1.8	1 4	1.5	0.0	-17	1.3	1.7	0.6	-0.2	0.1	
2011-02	1 1	0.0	0.3	0.2	-1.3	0.0	-0.2	-2.0	-0.4	0.3	-1.2	-1.2	-0.3	-0.1	-1.0	-0.7	-0.1	
2011-Q3	-14	-1.6	-17	1.0	-5.5	-2.9	-3.7	-3.3	-2.4	-1.0	-1.5	0.0	-3.1	-2.8	-2.8	-1 1	1.6	
2011-Q4	-1.3	-1.5	-2.3	0.5	-4.2	-2.9	-6.1	-4.4	-1.5	-1.3	-2.5	-0.3	-4.0	-4.0	-3.5	-2.8	-0.4	
2012-Q1	1.0	-0.1	1.0	1.0	-0.1	0.4	-3.8	-2.3	1.5	-0.4	-1.6	0.1	-1.0	-1.3	-3.1	-2.0	-0.8	
2012-Q2	0.9	-0.7	0.6	1.3	0.7	0.9	-3.2	-3.3	0.6	-0.4	-0.7	0.5	-0.6	-1.1	-2.9	-2.4	1.1	
2012-Q3	-0.9	-1.1	-0.6	1.1	-0.9	-0.2	-2.4	-3.3	-0.4	-1.0	0.2	-1.1	-2.4	-2.0	-2.8	-3.3	1.2	
2012-Q4	0.0	0.5	0.5	1.3	1.7	1.1	0.0	-0.8	1.3	-0.4	1.1	-0.8	-1.0	-0.9	-2.7	-2.1	1.0	
2013-Q1	0.7	0.7	0.2	1.8	1.5	0.9	-0.5	-0.8	1.8	0.2	0.8	3.5	1.2	-1.6	-1.8	-1.4	1.0	
2013-Q2	0.3	0.5	-0.4	-0.2	1.1	0.8	-1.1	-0.8	1.5	-0.7	0.1	6.0	0.6	-2.0	-2.0	-1.6	1.3	
2013-Q3	0.5	0.9	0.3	-1.1	0.9	1.6	-0.2	-0.2	1.5	-0.6	-2.1	1.8	1.2	-0.8	-1.6	-2.7	-0.5	
2013-Q4	1.9	1.2	0.1	0.0	2.0	0.8	1.8	2.1	1.7	0.5	-2.0	-1.0	2.3	0.1	-1.3	-2.4	-1.5	
2014-Q1	2.1	0.9	0.6	-0.4	0.6	0.8	2.4	2.2	1.3	-0.2	-2.4	0.9	1.4	-0.6	-1.2	-2.0	-0.3	
2014-Q2	1.7	1.0	0.4	1.0	-0.2	0.3	1.7	1.0	1.0	-1.1	-0.8	-3.7	0.9	-1.8	-1.4	-1.9	0.4	
2014-Q3	2.9	1.1	0.7	2.1	1.1	-0.9	0.3	0.6	1.8	-0.8	1.4	-4.6	1.0	-1.1	-1.0	-1.0	-0.4	
2014-Q4	3.4	-0.6	0.6	0.2	-0.9	-0.7	-1.1	-0.4	0.2	-1.1	-0.2	1.0	-0.6	-1.4	-0.3	-1.1	-1.3	
2015-Q1	3.0	-2.1	-3.2	-0.4	0.5	1.0	1.2	0.3	0.2	-2.2	-0.4	1.1	-0.2	-1.8	0.2	-1.4	-1.2	
2015-Q2	2.6	-1.0	-4.5	0.8	2.3	1.8	4.1	1.8	2.0	-2.5	-1.1	0.8	1.0	-0.6	1.7	-1.7	-1.0	
2015-Q3	1.6	-0.5	-4.6	0.5	0.0	-1.2	2.4	1.0	-0.1	-4.1	-2.1	-0.6	-0.8	-1.0	-0.3	-2.3	-2.0	
2015-Q4	1.2	-0.9	-5.0	-0.1	-1.1	-1.4	0.5	-0.1	-0.8	-4.5	-1.8	-2.1	-1.2	-0.6	-1.1	-3.0	-1.7	
2016-Q1	0.9	-0.6	-4.5	-0.2	0.1	-1.4	-1.4	-0.6	-0.4	-3.6	-1.4	-3.3	-0.9	-1.5	-0.9	-3.6	-0.1	
2016-Q2	1.9	0.6	-3.4	0.2	0.5	-1.9	-1.4	-0.2	0.6	-2.5	-0.3	-2.9	-0.1	-1.8	-1.0	-3.5	0.6	0.6
2016-Q3	3.3	1.5	-1.5	1.4	-0.8	-0.7	0.3	1.1	2.7	-2.2	0.0	-1.6	0.3	-0.7	-0.4	-2.4	1.2	1.0
2016-Q4	2.3	1.5	-1.4	0.6	0.9	0.6	0.8	1.6	2.9	-2.0	-0.5	-0.1	1.0	-1.0	0.6	-2.6	0.7	1.5
06/23/16	0.4	1.6	-2.7	0.0	-1.0	-0.7	1.3	0.5	-0.4	-2.6	-0.6	-1.1	0.0	-1.3	-0.3	-4.1	-0.5	-0.4
06/27/16	-0.8	0.9	-3.4	-0.7	-2.8	-2.2	-0.6	-1.2	-1.9	-3.3	-1.0	-1.8	-0.7	-1.9	-0.6	-4.5	-0.7	-3.6
11/04/16	0.2	2.1	0.3	0.1	-1.0	-0.3	0.2	0.4	0.8	-2.2	-1.2	-0.5	-0.2	-1.3	0.4	-3.5	0.6	-0.4
vg Q4 201	2.3	1.5	-1.4	0.6	0.9	0.6	0.8	1.6	2.9	-2.0	-0.5	-0.1	1.0	-1.0	0.6	-2.6	0.7	1.5
12/30/16	3.0	2.3	-1.1	0.2	2.1	1.7	2.1	2.2	3.8	-0.5	-0.4	0.8	1.8	-0.9	0.8	-2.4	0.7	2.2
07/07/17	3.2	3.2	1.5	1.1	1.9	3.2	3.3	2.7	3.2	-1.3	1.9	1.3	1.8	2.1	0.1	-1.2	1.7	2.4
08/24/17	3.1	3.3	3.8	1.5	1.6	2.5	3.7	2.6	3.1	-0.8	3.0	0.9	2.1	2.1	-0.2	-1.2	1.9	2.5
Country	United S	Canada B	razil	Mexico	France	Germany	Italy	Spain	UK FTSE 10	Russia	Turkey	Japan /	Australia	South Kc	China	India	Indonesia	UK FTSE 250

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Douglas T. Breeden is the William W. Priest Professor of Finance and former Dean of Duke University's Fuqua School of Business. He also served on faculties at Chicago Booth, Stanford and North Carolina, where he was the Dalton McMichael Professor of Finance. He was the Fischer Black Visiting Professor of Financial Economics at MIT's Sloan School in 2011-2013, winning an "Outstanding Teacher" award.

Breeden published seminal research on insurance prices implicit in option prices, the Consumption CAPM, and hedging mortgage securities. His current research is "A Stocks, Bonds, Consumers Leading Indicator" and (with Robert Litzenberger) "Central Bank Policy Impacts on the Distribution of Future Interest Rates," which won a Roger Murray Prize from the Q-Group. He has presented this research to central bank meetings in the USA, England, France, Italy, Hong Kong, Singapore, Cambodia, Thailand, Taiwan, Brunei, and Malaysia, as well as at the International Monetary Fund in Washington, D.C..

Breeden was Associate Editor of 5 top journals. He was Founding Editor and Editor for 10 years of the <u>Journal of Fixed Income</u>. He was elected to the Board of Directors of the American Finance Association and in 2010 a lifetime Fellow. The International Association for Quantitative Finance named Breeden "Financial Engineer of the Year 2013" for being an "industry pioneer."

Breeden holds a Ph.D. in Finance from Stanford and an S.B. from M.I.T. He served on the MIT President's Council, the Sloan School Visiting Committee and the Stanford Business School Advisory Council. He was named an Honorary Professor of the Chinese Academy of Sciences and served on the Boards of Goethe Business School in Germany and the Financial Management Association. He is on the Board of Trustees of Commonfund and is a Senior Research Consultant for Amundi Smith Breeden, a money management firm he co-founded.

During his career, Breeden has been active in philanthropy. He provided naming grants for Breeden Hall and the Breeden Professorship at Duke's Fuqua School of Business, the Breeden Conference Room at MIT Sloan, Breeden Theater at Episcopal High School and the Breeden Memorial Library in his hometown of Leavenworth, Indiana.