

Name: _____

Mixed Numbers to Improper Fractions

We've seen that a mixed number can be written as an improper fraction, and an improper fraction can be written as a mixed number. How do you go about changing one into the other?

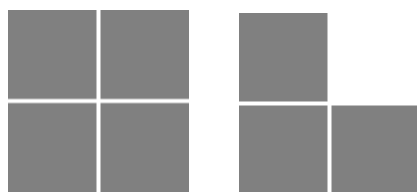
We'll start with converting (changing) mixed numbers to improper fractions.

Suppose we want to change the mixed number $1\frac{3}{4}$ to an improper fraction.

First let's draw a picture.

Here we have $1\frac{3}{4}$ large squares.

We start by dividing the 1 whole square into 4 fourths.

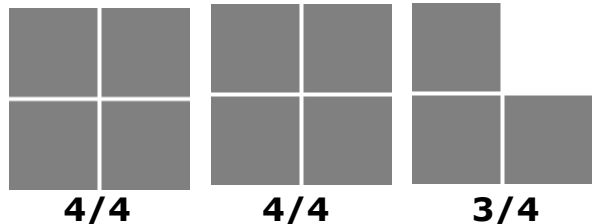


Now we count up the pieces. There are 7 pieces.

Each piece is $\frac{1}{4}$ of a square. So that's $7 \times \frac{1}{4} = \frac{7}{4}$ squares.

So, $1\frac{3}{4} = \frac{7}{4}$.

Instead, what if had wanted to change $2\frac{3}{4}$ to an improper fraction? Then we would have drawn 2 whole squares, and cut each of them into fourths.



How many fourths do we have this time? 4 from each of the 2 whole squares plus 3 more.

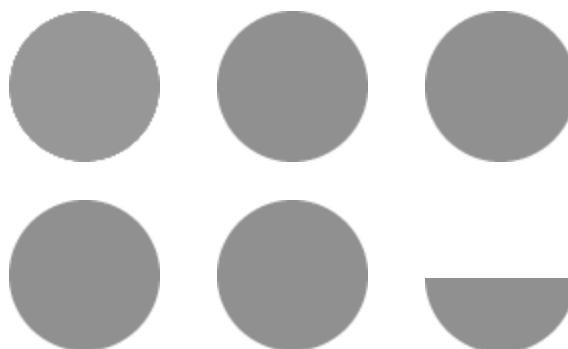
$$\frac{4}{4} + \frac{4}{4} + \frac{3}{4} = \frac{11}{4}, \quad \text{or}$$

$$(2 \times \frac{4}{4}) + \frac{3}{4} = \frac{8}{4} + \frac{3}{4} = \frac{11}{4}.$$

$$2\frac{3}{4} = \frac{11}{4}$$

1. Here are $5\frac{1}{2}$ circles.

Change $5\frac{1}{2}$ to an improper fraction.



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Mixed Numbers to Improper Fractions

Now let's do one without the pictures.

Let's convert $3 \frac{2}{5}$ to an improper fraction.

How? We'll change the 3 wholes into fifths and add on the $\frac{2}{5}$.

Each whole is $\frac{5}{5}$. So 3 wholes are $\frac{5}{5} + \frac{5}{5} + \frac{5}{5} = (3 \times \frac{5}{5}) = \frac{15}{5}$.

Now we add on the $\frac{2}{5}$ to the $\frac{15}{5}$. $\frac{15}{5} + \frac{2}{5} = \frac{17}{5}$.

Do you see what's going on?

The denominator (bottom) of your improper fraction will be the SAME as the denominator of the fractional part of the mixed number.

To get the numerator of the improper fraction, you multiply whole part of the mixed number by the denominator of the fractional part and add on the numerator of the fractional part.

Now, let's change $2 \frac{5}{6}$ to an improper fraction.

<p>① $2 \frac{5}{6}$</p> <p style="text-align: center;">↑ ↑</p> <p style="text-align: center;">multiply these...</p> <p style="text-align: center;">2×6</p>	<p>② $2 \frac{5}{6}$ ← then add this to the product</p> <p style="text-align: center;">$2 \times 6 + 5$</p>
<p>③ $2 \times 6 + 5 = 17$</p> <p style="text-align: center;">↑</p> <p style="text-align: center;">this is your new numerator</p>	

You keep the same denominator. So ... $2 \frac{5}{6} = \frac{17}{6}$

2. Change the following mixed numbers to improper fractions:

$$3 \frac{2}{3}$$

$$4 \frac{1}{4}$$

$$2 \frac{5}{8}$$