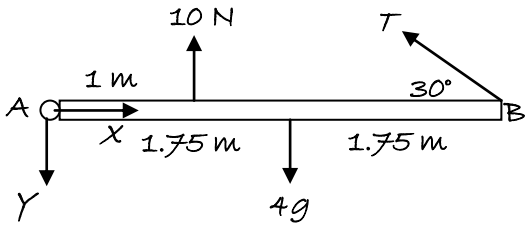
Section 2: Moments of forces at an angle

Solutions to Exercise level 2

1. (i) Moment $= 5 \times 0.25 = 1.25$ Nm
(ii) The line of action of the force must remain tangential to the steering wheel.

2.



Taking moments about A: $T \sin 30° \times 3.5 - 4g \times 1.75 + 10 \times 1 = 0$

$1.75T = 58.6$

$T = 33.5$ (3 s.f.)

Resolving vertically: $10 - Y + T \sin 30° - 4g = 0$

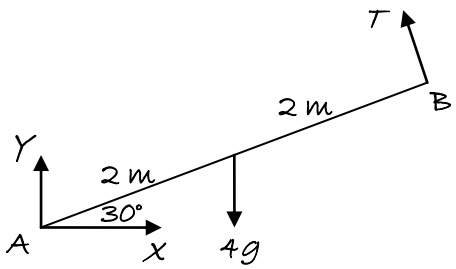
$Y = 10 + 33.486 \times \frac{1}{2} - 39.2 = -12.457$

Resolving horizontally: $X - T \cos 30° = 0$

$X = 33.486 \cos 30° = 28.999$

Magnitude of reaction force $= \sqrt{12.457^2 + 28.999^2} = 31.6$ N (3 s.f.)

3.



Taking moments about A: $4T - 4g \cos 30° \times 2 = 0$

$T = g\sqrt{3}$

$T = 16.97$ N (2 d.p.)

Resolving vertically: $Y - 4g + T \cos 30° = 0$

$Y = 4g - g\sqrt{3} \times \frac{\sqrt{3}}{2} = 2.5g$

Resolving horizontally: $X - T \sin 30° = 0$

$X = \frac{1}{2} g\sqrt{3}$

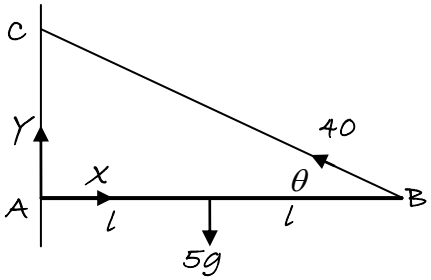
Magnitude of reaction $= g\sqrt{2.5^2 + \left(\frac{1}{2}\sqrt{3}\right)^2} = 25.9$ N (3 s.f.)

$\tan\theta = \frac{Y}{X} = \frac{2.5}{\frac{1}{2}\sqrt{3}}$

$\theta = 70.9°$

The direction of the reaction force is 70.9° above the horizontal

4.

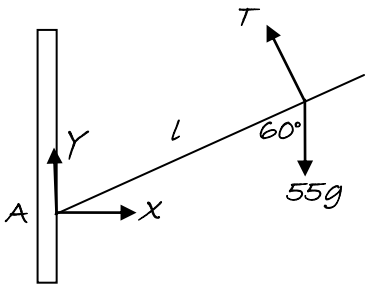


Taking moments about A: $40\sin\theta \times 2l - 5g \times l = 0$

$\sin\theta = \frac{5g}{80}$

$\theta = 37.8°$

5.



Taking moments about A:

$T\,l - 55g\sin 60° \times l = 0$

$T = 55g\sin 60° = 27.5g\sqrt{3} = 467$ N (3 s.f.)

Resolving horizontally: $X - T\cos 60° = 0$

$X = 27.5g\sqrt{3} \times \frac{1}{2} = 13.75g\sqrt{3}$

Resolving vertically: $Y + T\sin 60° - 55g = 0$

$Y = 55g - 27.5g\sqrt{3} \times \frac{\sqrt{3}}{2} = 13.75g$

Reaction force $= g\sqrt{(13.75\sqrt{3})^2 + (13.75)^2} = 269.5$ N

$\tan\theta = \frac{Y}{X} = \frac{13.75g}{13.75g\sqrt{3}} = \frac{1}{\sqrt{3}}$

$\theta = 30°$

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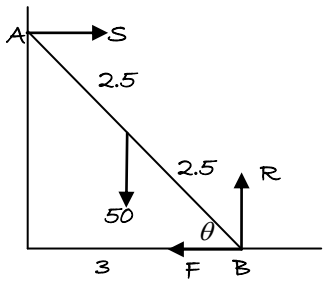
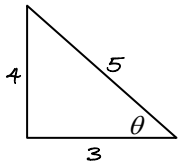
6.





Resolving vertically: $R - 50 = 0$

$R = 50$

Taking moments about A: $50\cos\theta \times 2.5 + F\sin\theta \times 5 - R\cos\theta \times 5 = 0$

$$50 \times \frac{3}{5} \times 2.5 + F \times \frac{4}{5} \times 5 - 50 \times \frac{3}{5} \times 5 = 0$$

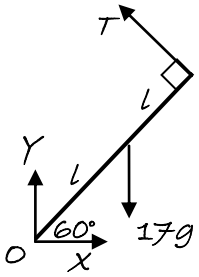
$75 + 4F - 150 = 0$

$4F = 75$

$F = 18.75$

The frictional force is 18.75 N.

7. (i)



Taking moments about O: $T \times 2l - 17g\cos 60° \times l = 0$

$2T = 17g \times \frac{1}{2}$

$T = 41.65$

Tension in rope is 41.65 N

Resolving horizontally: $X - T\sin 60° = 0$

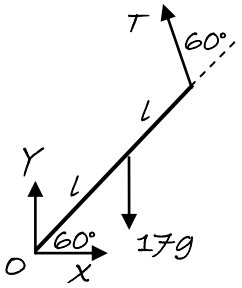
$$X = 41.65 \times \frac{\sqrt{3}}{2} = 20.825\sqrt{3}$$

Resolving vertically: $Y + T\cos 60° - 17g = 0$

$Y = 17 \times 9.8 - 41.65 \times \frac{1}{2} = 145.775$

Reaction force $= \sqrt{\left(20.825\sqrt{3}\right)^2 + 145.775^2} = 150$ N (3 s.f.)

(ii)



Taking moments about O: $T \times 2l \sin 60° - 17g \cos 60° \times l = 0$

$$2T \times \tfrac{1}{2}\sqrt{3} = 17g \times \tfrac{1}{2}$$

$$T = \frac{83.3}{\sqrt{3}} = 48.1$$

Tension in rope is 48.1 N (3 s.f.)

Resolving horizontally: $X - T \sin 30° = 0$

$$X = \frac{83.3}{\sqrt{3}} \times \frac{1}{2} = \frac{41.65}{\sqrt{3}}$$

Resolving vertically: $Y + T \cos 30° - 17g = 0$

$$Y = 17 \times 9.8 - \frac{83.3}{\sqrt{3}} \times \frac{\sqrt{3}}{2} = 124.95$$

Reaction force $= \sqrt{\left(\frac{41.65}{\sqrt{3}}\right)^2 + 124.95^2} = 127$ N (3 s.f.)