

Section 1: Definitions and notation

Solutions to Exercise level 2

1. (i) Terms are of the form $2k$.
The last term is the 10th term.
The series can be written as $\sum_1^{10} 2k$.
- (ii) Terms are of the form k^2 .
The last term is the 12th term.
The series can be written as $\sum_1^{12} k^2$.
- (iii) Terms are of the form $\frac{1}{k}$.
The last term is the 20th term.
The series can be written as $\sum_1^{20} \frac{1}{k}$.
- (iv) Terms are of the form $(-2)^{k-1}$.
The last term is the 7th term.
The series can be written as $\sum_1^7 (-2)^{k-1}$.
2. (i) $\sum_1^5 (2k+1) = 3 + 5 + 7 + 9 + 11 = 35$
- (ii) $\sum_1^4 k^2 = 1 + 4 + 9 + 16 = 30$
- (iii) $\sum_0^4 2^k = 1 + 2 + 4 + 8 + 16 = 31$
3. (i) $\sum_1^6 (2k^2 - 1) = 1 + 7 + 17 + 31 + 49 + 71$
 $= 176$
- (ii) $\sum_1^5 r^2 - \sum_0^3 \frac{r}{r+1} = (1 + 4 + 9 + 16 + 25) - (0 + \frac{1}{2} + \frac{2}{3} + \frac{3}{4})$
 $= 53 \frac{1}{12} = \frac{637}{12}$

Edexcel A level Maths Sequences 1 Exercise solutions

$$\begin{aligned} \text{(iii)} \quad \sum_0^4 (2k+1) - \sum_0^4 (2k-1) &= (1+3+5+7+9) - (-1+3+5+7+9) \\ &= 10 \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad \sum_1^5 r^2 + \sum_1^5 (2r+1) &= (1+4+9+16+25) + (3+5+7+9+11) \\ &= 90 \end{aligned}$$

$$\begin{aligned} 4. \text{ (iii)} \quad \sum_0^4 (2k+1) - \sum_0^4 (2k-1) &= \sum_0^4 ((2k+1) - (2k-1)) \\ &= \sum_0^4 2 \\ &= 2+2+2+2+2 \\ &= 10 \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad \sum_1^5 r^2 + \sum_1^5 (2r+1) &= \sum_1^5 (r^2 + 2r + 1) \\ &= \sum_1^5 (r+1)^2 \\ &= 4+9+16+25+36 \\ &= 90 \end{aligned}$$