

Section 1: Introduction to differential equations

Exercise level 1

- 1. Formulate a first order differential equation between the variables *x* and *t* (time) from the following information:
 - (i) The rate of change of x is inversely proportional to the cube of the time t.
 - (ii) The rate of decrease of x is directly proportional to the square root of x.
- 2. Find the general solution for each of the following differential equations.

(i)
$$\frac{dy}{dx} = 3x^2 + 2$$

(ii)
$$2\frac{dy}{dx} - x = 10$$

(iii)
$$x^2 \frac{dy}{dx} = 3 + x$$

3. By separating the variables, find the general solution of each of the following differential equations, giving y in terms of x.

(i)
$$\frac{dy}{dx} = y^2$$

(ii) $\frac{dy}{dx} = 2xy^2$
(iii) $\frac{dy}{dx} = 2xy$

