

Section 1: The general binomial expansion

Exercise level 2

1. Expand each of the following functions in ascending powers of x up to the term in x^3 . In each case state the values of x for which the expansion is valid.

(i)
$$\frac{1}{3-x}$$

(ii)
$$\sqrt{4-3x}$$

(iii)
$$\frac{2+x}{2-x}$$

(iv)
$$\sqrt{\frac{1-x}{1-2x}}$$

2. (i) Write out the first three terms in the expansion of $\frac{1}{\sqrt{1-2x}}$.

- (ii) Show that $\frac{1}{\sqrt{0.8}} = \frac{\sqrt{5}}{2}$.
- (iii)By substituting x = 0.1 in your expansion from (i), and using your result from (ii), find an approximate value for $\sqrt{5}$.
 - (iv) Find the percentage error in your answer from (iii).

