

**Topic assessment**

1. A line  $l_1$  has equation  $5y + 4x = 3$ .
  - (i) Find the gradient of the line. [1]
  - (ii) Find the equation of the line  $l_2$  which is parallel to  $l_1$  and passes through the point  $(1, -2)$ . [3]
2. Describe fully the curve whose equation is  $x^2 + y^2 = 4$ . [2]
3. The coordinates of two points are A  $(-1, -3)$  and B  $(5, 7)$ . Calculate the equation of the perpendicular bisector of AB. [4]
4. Show that the line  $y = 3x - 10$  is a tangent to the circle  $x^2 + y^2 = 10$ . [4]
5. The line  $y = 2x - 3$  meets the  $x$ -axis at the point P, and the line  $3y + 4x = 8$  meets the  $x$ -axis at the point Q. The two lines intersect at the point R.
  - (i) Find the coordinates of R. [4]
  - (ii) Find the area of triangle PQR. [3]
6. The equation of a circle is  $x^2 + y^2 - 4x + 2y = 15$ 
  - (i) Find the coordinates of the centre C of the circle, and the radius of the circle. [3]
  - (ii) Show that the point P  $(4, -5)$  lies on the circle. [1]
  - (iii) Find the equation of the tangent to the circle at the point P. [4]
7. The coordinates of four points are P  $(-2, -1)$ , Q  $(6, 3)$ , R  $(9, 2)$  and S  $(1, -2)$ .
  - (i) Calculate the gradients of the lines PQ, QR, RS and SP. [4]
  - (ii) What name is given to the quadrilateral PQRS? [1]
  - (iii) Calculate the length SR. [2]
  - (iv) Show that the equation of SR is  $2y = x - 5$  and find the equation of the line  $L$  through Q perpendicular to SR. [5]
  - (v) Calculate the coordinates of the point T where the line  $L$  meets SR. [3]
  - (vi) Calculate the area of the quadrilateral PQRS. [3]
8. AB is the diameter of a circle. A is  $(1, 3)$  and B is  $(7, -1)$ .
  - (i) Find the coordinates of the centre C of the circle. [2]
  - (ii) Find the radius of the circle. [2]
  - (iii) Find the equation of the circle. [2]
  - (iv) The line  $y + 5x = 8$  cuts the circle at A and again at a second point D. Calculate the coordinates of D. [4]
  - (v) Prove that the line AB is perpendicular to the line CD. [3]

**Total 60 marks**

# Edexcel AS Maths Coordinate geometry Assessment solutions

## Solutions to topic assessment

1. (i)  $5y + 4x = 3$  .

$$5y = -4x + 3$$

$$y = -\frac{4}{5}x + \frac{3}{5}$$

$$\text{Gradient of line} = -\frac{4}{5}$$

[1]

(ii)  $l_2$  is parallel to  $l_1$ , so it has gradient  $-\frac{4}{5}$ .

$$\text{Equation of line is } y - (-2) = -\frac{4}{5}(x - 1)$$

$$5(y + 2) = -4(x - 1)$$

$$5y + 10 = -4x + 4$$

$$5y + 4x + 6 = 0$$

[3]

2. The curve is a circle, centre  $O$  and radius 2.

[2]

$$3. \text{ Gradient of } AB = \frac{y_1 - y_2}{x_1 - x_2} = \frac{-3 - 7}{-1 - 5} = \frac{-10}{-6} = \frac{5}{3}$$

$$\text{Gradient of line perpendicular to } AB = -\frac{3}{5}.$$

$$\text{The line passes through the midpoint of } AB = \left( \frac{-1 + 5}{2}, \frac{-3 + 7}{2} \right) = (2, 2)$$

$$\text{Equation of line is } y - 2 = -\frac{3}{5}(x - 2)$$

$$5(y - 2) = -3(x - 2)$$

$$5y - 10 = -3x + 6$$

$$5y + 3x = 16$$

[4]

4. Substituting  $y = 3x - 10$  into  $x^2 + y^2 = 10$

$$\text{gives } x^2 + (3x - 10)^2 = 10$$

$$x^2 + 9x^2 - 60x + 100 = 10$$

$$10x^2 - 60x + 90 = 0$$

$$x^2 - 6x + 9 = 0$$

$$(x - 3)^2 = 0$$

Since the equation has a repeated root, the line meets the circle just once, and so the line is a tangent to the circle.

[4]

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5. (i) Substituting  $y = 2x - 3$  into  $3y + 4x = 8$ :

$$3(2x - 3) + 4x = 8$$

$$6x - 9 + 4x = 8$$

$$10x = 17$$

$$x = 1.7$$

When  $x = 1.7$ ,  $y = 2 \times 1.7 - 3 = 3.4 - 3 = 0.4$

The coordinates of R are (1.7, 0.4)

[4]

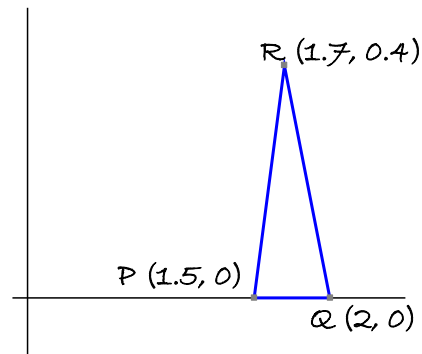
(ii) P is the point on  $y = 2x - 3$  where  $y = 0$ , so P is (1.5, 0)

Q is the point on  $3y + 4x = 8$  where  $y = 0$ , so Q is (2, 0).

Area =  $\frac{1}{2} \times \text{base} \times \text{height}$

$$= \frac{1}{2} \times 0.5 \times 0.4$$

$$= 0.1$$



[3]

6. (i)  $x^2 + y^2 - 4x + 2y = 15$

$$x^2 - 4x + y^2 + 2y = 15$$

$$(x - 2)^2 - 4 + (y + 1)^2 - 1 = 15$$

$$(x - 2)^2 + (y + 1)^2 = 20$$

The centre C of the circle is (2, -1) and the radius is  $\sqrt{20}$ .

[3]

(ii) Substituting  $x = 4$  and  $y = -5$ :  $(4 - 2)^2 + (-5 + 1)^2 = 4 + 16 = 20$   
so the point (4, -5) lies on the circle.

[1]

(iii) Gradient of CP =  $\frac{-1 - (-5)}{2 - 4} = \frac{4}{-2} = -2$

Tangent at P is perpendicular to CP, so gradient of tangent =  $\frac{1}{2}$ .

Equation of tangent is  $y - (-5) = \frac{1}{2}(x - 4)$

$$2(y + 5) = x - 4$$

$$2y + 10 = x - 4$$

$$2y = x - 14$$

[4]

7. (i) Gradient of PQ =  $\frac{y_1 - y_2}{x_1 - x_2} = \frac{-1 - 3}{-2 - 6} = \frac{-4}{-8} = \frac{1}{2}$

Gradient of QR =  $\frac{y_1 - y_2}{x_1 - x_2} = \frac{3 - 2}{6 - 9} = \frac{1}{-3} = -\frac{1}{3}$

Gradient of RS =  $\frac{y_1 - y_2}{x_1 - x_2} = \frac{2 - (-2)}{9 - 1} = \frac{4}{8} = \frac{1}{2}$

Gradient of SP =  $\frac{y_1 - y_2}{x_1 - x_2} = \frac{-2 - (-1)}{1 - (-2)} = \frac{-1}{3} = -\frac{1}{3}$

[4]

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(ii) PQ is parallel to RS, and QR is parallel to SP, so the quadrilateral is a parallelogram.

[1]

$$(iii) SR = \sqrt{(9-1)^2 + (2-(-2))^2} = \sqrt{64+16} = \sqrt{80}$$

[2]

(iv) From (i), gradient of SR =  $\frac{1}{2}$

$$\text{Equation of SR is } y - (-2) = \frac{1}{2}(x - 1)$$

$$2(y + 2) = x - 1$$

$$2y + 4 = x - 1$$

$$2y = x - 5$$

Line perpendicular to SR has gradient -2

Line L has gradient -2 and goes through (6, 3)

$$\text{Equation of L is } y - 3 = -2(x - 6)$$

$$y - 3 = -2x + 12$$

$$y + 2x = 15$$

[5]

(v) Equation of L is  $y = 15 - 2x$

Substituting into equation of SR gives  $2(15 - 2x) = x - 5$

$$30 - 4x = x - 5$$

$$35 = 5x$$

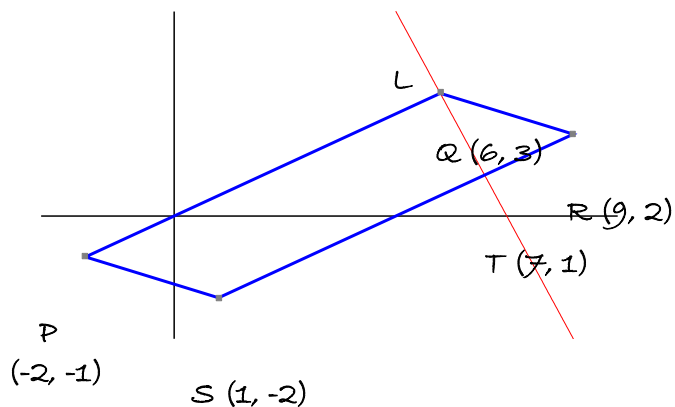
$$x = 7$$

When  $x = 7$ ,  $y = 15 - 2 \times 7 = 1$

Coordinates of T are (7, 1)

[3]

(vi)



$$\text{Length QT} = \sqrt{(7-6)^2 + (1-3)^2} = \sqrt{1+4} = \sqrt{5}$$

$$\text{Area of parallelogram} = SR \times QT$$

$$= \sqrt{80} \sqrt{5}$$

$$= \sqrt{16} \sqrt{5} \sqrt{5}$$

$$= 4 \times 5 = 20$$

[3]

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8. (i) C is the midpoint of AB.

$$C = \left( \frac{1+7}{2}, \frac{3+(-1)}{2} \right) = (4, 1)$$

[2]

(ii) Radius of circle = CA =  $\sqrt{(4-1)^2 + (1-3)^2} = \sqrt{9+4} = \sqrt{13}$

[2]

(iii) Equation of circle is  $(x-4)^2 + (y-1)^2 = 13$

[2]

(iv) Substituting  $y = -5x + 8$  into equation of circle:

$$(x-4)^2 + (-5x+8-1)^2 = 13$$

$$(x-4)^2 + (-5x+7)^2 = 13$$

$$x^2 - 8x + 16 + 25x^2 - 70x + 49 = 13$$

$$26x^2 - 78x + 52 = 0$$

$$x^2 - 3x + 2 = 0$$

$$(x-1)(x-2) = 0$$

$$x = 1 \text{ or } x = 2$$

$x = 1$  is point A, so point D is  $x = 2$

When  $x = 2$ ,  $y = -5 \times 2 + 8 = -2$

The coordinates of D are (2, -2)

[4]

(v) Gradient of AB =  $\frac{3-(-1)}{1-7} = \frac{4}{-6} = -\frac{2}{3}$

Gradient of CD =  $\frac{1-(-2)}{4-2} = \frac{3}{2}$

Gradient of AB  $\times$  gradient of CD =  $-\frac{2}{3} \times \frac{3}{2} = -1$

so AB is perpendicular to CD.

[3]