## Advanced Mathematics <br> Support Programme ${ }^{\circ}$

## Edexcel A Level FM Revision Questions

## Integration

## Question 1

(i) Determine $\int \frac{2 x^{2}-x+5}{(x-3)(x+2)^{2}} \mathrm{~d} x$
(ii) Determine $\int_{0}^{\sqrt{2}} \frac{(x+1)\left(x^{2}+1\right)}{(x+2)\left(x^{2}+2\right)} \mathrm{d} x$

## Question 2

Determine the following integrals, using a substitution if necessary:
(i) $\int \frac{\mathrm{e}^{x}}{\mathrm{e}^{2 x}+1} \mathrm{~d} x$
(ii) $\int \frac{x}{1+x^{4}} \mathrm{~d} x$
(iii) $\int \frac{1}{x^{2}+6 x+18} \mathrm{~d} x$
(iv) $\int \frac{1}{\left(2 x^{2}+3\right)^{\frac{3}{2}}} \mathrm{~d} x$
(v) $\int \frac{4 x+5}{\sqrt{4-6 x-x^{2}}} \mathrm{~d} x$

## Question 3

The region between the line $y=6-2 x$ and the curve $y=\frac{4}{x}$ is rotated about the $y$-axis through $360^{\circ}$. Find the exact volume generated.

## Question 4

The region between the parabola $y^{2}=4 x$, the $x$-axis and the line $x=1$ is rotated about the $x$-axis through $360^{\circ}$.
(i) Find the exact volume generated:
(a) by integrating with respect to $x$
(b) by integrating with respect to the parameter $t$, where $x=t^{2}$ and $y=2 t$.
(ii) Use the mean value of the function to carry out a rough check on your answer in (i).

