

Edexcel A Level FM Revision Questions

Integration

Question 1

(i) Determine $\int \frac{2x^2 - x + 5}{(x - 3)(x + 2)^2} dx$

(ii) Determine
$$\int_0^{\sqrt{2}} \frac{(x+1)(x^2+1)}{(x+2)(x^2+2)} dx$$

Question 2

Determine the following integrals, using a substitution if necessary:

(i)
$$\int \frac{\mathrm{e}^x}{\mathrm{e}^{2x} + 1} \mathrm{d}x$$

(ii)
$$\int \frac{x}{1+x^4} dx$$

(iii)
$$\int \frac{1}{x^2 + 6x + 18} \mathrm{d}x$$

(iv)
$$\int \frac{1}{(2x^2+3)^{\frac{3}{2}}} dx$$

(v)
$$\int \frac{4x+5}{\sqrt{4-6x-x^2}} \, \mathrm{d}x$$

Question 3

The region between the line y = 6 - 2x and the curve $y = \frac{4}{x}$ is rotated about the y-axis through 360°. Find the exact volume generated.

Question 4

The region between the parabola $y^2 = 4x$, the x-axis and the line x = 1 is rotated about the x-axis through 360°.

- (i) Find the exact volume generated:
 - (a) by integrating with respect to x
 - (b) by integrating with respect to the parameter *t*, where $x = t^2$ and y = 2t.
- (ii) Use the mean value of the function to carry out a rough check on your answer in (i).