Edexcel AS Further Mathematics Matrices



Section 2: Matrices and transformations

Exercise level 2

1. Plot the object and image for each of the following on the same diagram and describe each as a single transformation.

Object Matrix
(i)
$$P(4, 2) Q(4, 4) R(0, 4)$$

$$\begin{pmatrix}
-0.5 & 0 \\
0 & -0.5
\end{pmatrix}$$
(ii) $P(-6, 8) Q(-2, 8) R(-2, 6)$

$$\begin{pmatrix}
0 & -1 \\
-1 & 0
\end{pmatrix}$$

- 2. Draw a quadrilateral with vertices A(3, 4) B(4, 0) C(3, 1) D (0, 0) and find its image under the transformation $\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$. Describe the transformation, and find the ratio of the image area to object area.
- 3. Find the images of A(3, 1) B(3, 3) C(6, 3) D(6, 1) under the transformation $\begin{pmatrix} 1 & 0 \\ -2 & 1 \end{pmatrix}$. Show ABCD and its image on a diagram.
- 4. The transformation R is an anticlockwise rotation about the origin through an angle of 60^{0} . Find the matrix **R** using exact values only.
- 5. Find the matrices which represent the following transformations in three dimensions.
 - (i) rotation of 90° about the z-axis
 - (ii) reflection in y = 0.
- 6. The following matrices represent a rotation about the origin. Find the angle and direction of rotation in each case

(i)
$$\begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$$
 (ii) $\begin{pmatrix} -0.8 & -0.6 \\ 0.6 & -0.8 \end{pmatrix}$

- 7. Find 2×2 matrices to represent the transformation P, which is a reflection in the y-axis, and the transformation Q, which is a rotation of 90° clockwise about the origin. Hence find a single matrix to represent a reflection in the y-axis followed by a rotation of 90° clockwise about the origin. Describe this as a single transformation.
- 8. Draw diagrams to show the effect on the square with vertices O(0, 0) A(1, 0) B(1, 1) C(0, 1) of the matrices **R**, **S**, **RS** and **SR** given that $\mathbf{R} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$ and

Edexcel AS FM Matrices 2 Exercise

$$\mathbf{S} = \begin{pmatrix} 1 & -1 \\ 0 & 1 \end{pmatrix}.$$

- 9. (i) Draw triangle ABC such that A(2, 1) B(7, 1) and C(2, 4)
 - (ii) Find the image of ABC under the matrix $\begin{pmatrix} 1 & -1 \\ 1 & 1 \end{pmatrix}$ and plot the image on the same graph.
 - (iii) The transformation is a rotation followed by an enlargement. Calculate the angle of rotation and the scale factor of the enlargement.
- 10. (i) Write down a matrix S which represents a stretch, scale factor 3, in the x-direction.
 - (ii) The matrix \mathbf{T} is given by $\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$. The matrix \mathbf{M} represents the combined effect of the transformation represented by \mathbf{S} followed by the transformation represented by \mathbf{T} . Find \mathbf{M} .